

"Week 4" starts here.  
Other ~~the~~ scheme:

74.

Bipolar.

(Bipolar is not Polar) (!)

Also three levels:

+X ( $\rightarrow$  1)

0 ( $\equiv$  zero)

-X ( $\rightarrow$  1)

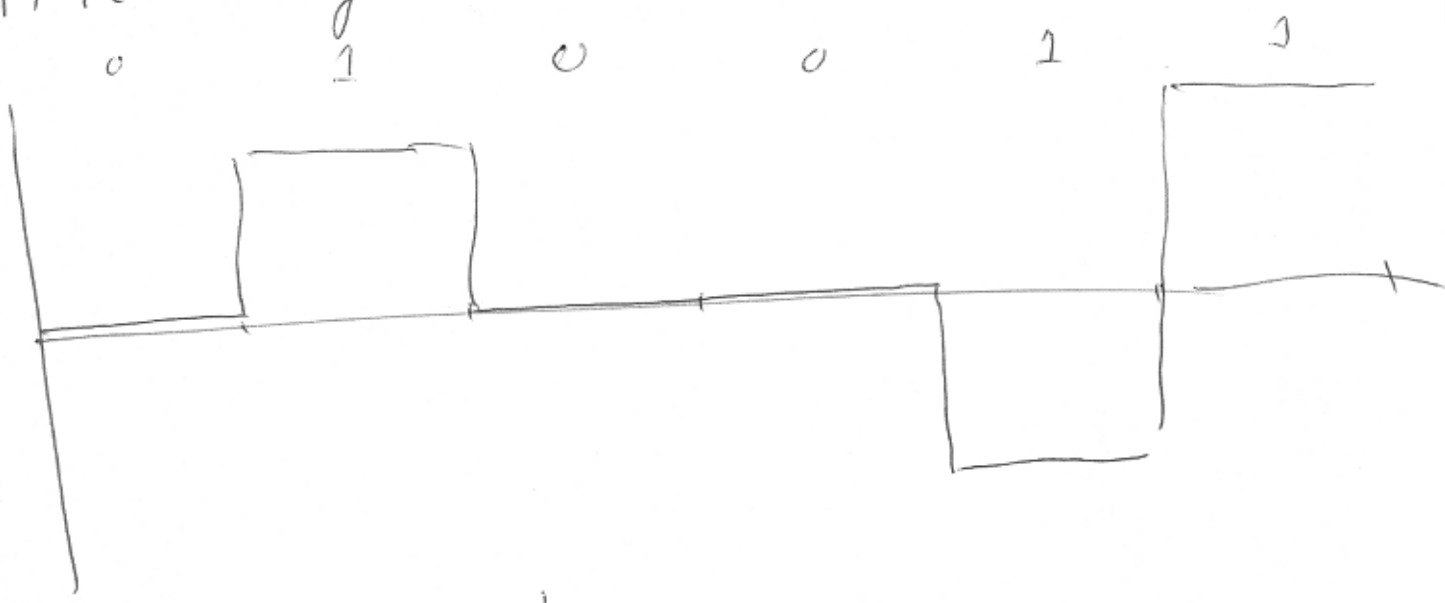
But 0 is not "intermediate<sup>ly</sup> state"

but used to represent zero.

1 is represented by +X as well as -X.

Bipolar A M I.

Alternating Mark Inversion.



etc.

There are more versions of Bipolar. Let's stop here.

To here 09/23/2003.

Next time:

$$(1-p) \sum_{k=1}^{\infty} k p^{k-1} = \frac{1}{1-p}$$

Start here 09/26/2003.

Last time we saw a number of ways to put a digital signal (bits) on a ~~two~~ pair of conductors (co-axial cable, twisted wire).

The examples I gave all are what is called Baseband.

Since last week I found out: in 802.3, 10 Base 5, 10 Base 2, 1 Base 5 and 100 Base T all use Manchester encoding.

There are other coding schemes: later. (Broadband, so called PSK encoding). (Also QAM etc.)

But First something else!

Number representations. (I assume you know this). 77

(1) One's complement:

In 8-bit representation:

$$\begin{aligned} 0000\ 0000 &= \text{zero} = +0 \\ 1111\ 1111 &= -\text{zero} = -0 \end{aligned}$$

$$\begin{aligned} 0000\ 0001 &= 1 \\ 1111\ 1110 &= -1 \end{aligned}$$

$$\begin{aligned} 0000\ 0010 &= 2 \\ 1111\ 1101 &= -2 \end{aligned}$$

⋮

$$\begin{aligned} 0111\ 1111 &= 1+2+4+8+\dots+2^6 = 2^7-1 = 127 \\ 1000\ 0000 &= -127 \end{aligned}$$

Similar for 16-bit representation

$$\left( \text{to } -(2^{15}-1) \text{ to } +(2^{15}-1) \right)$$

$$32 \text{ bit } \left( \text{to } -(2^{31}-1) \text{ to } +(2^{31}-1) \right)$$

etc

X is "one's complement" of  $-X$ .

# One's complement addition:

A: Add three bits:

three ~~all~~ zeros gives zero, no carry

2 zero, ~~one~~ 1 one gives 1, no carry

1 zero, 2 ones gives 0, carry 1

three ~~all~~ ones gives 1, carry 1

B. Add Two numbers: use A.

Example:

10 bit representation!

$$\begin{array}{r}
 1001001101 \\
 0011011110 \\
 \hline
 1100101011
 \end{array}$$

$\leftarrow$        $\leftarrow$   
 $\leftarrow$        $\leftarrow$   
 $\leftarrow$        $\leftarrow$

$$\begin{array}{l}
 (2^9 - 1) + (2^9 - 1) \\
 - (2^9 - 1) + (2^9 - 1)
 \end{array}$$

C. If less (left most) bits generate a carry: add to first (right most) bits.

6 bit repr

$$\begin{array}{r}
 110101 \\
 010001 \\
 \hline
 1 \boxed{000110} \rightarrow 000111
 \end{array}$$

$$1 \boxed{000111} \rightarrow \boxed{001000}$$

Result can be Wrong

Result can be wrong. (8 bit repr.)

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$$\begin{array}{r} 1000\ 0000 \quad (-128) \\ 1000\ 0000 \quad (-128) \\ \hline 0000\ 0001 \quad (+1) \end{array} +$$

should be  $-254$

difference:  $255 = 2^8 - 1$

~~0110~~

$$\begin{array}{r} 0100\ 0000 \quad (+64) \\ 0100\ 0000 \quad (+64) \\ \hline 1000\ 0000 \quad (-128) \end{array} +$$

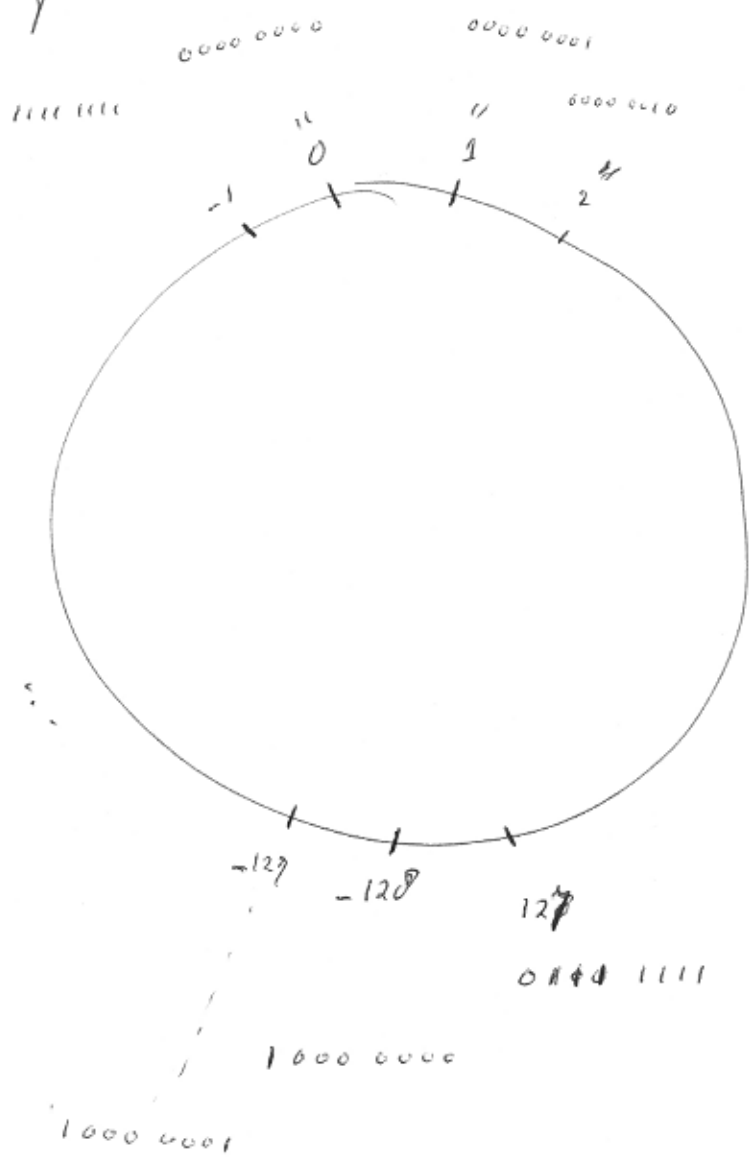
should be  $+128$

difference:  $255 = 2^8 - 1$

# Two's complement.

8 bits :  $2^8 = 256$  different numbers

Think of them in a circle :



Arithmetic: modulo  $2^8 = 256$   
Digital  $\rightarrow$  "decimal" :

- ① Compute as if it is an unsigned int.
- ② If  $0 \leq \text{value} \leq 127$  : that is the value
- If  $128 \leq \text{value} \leq 255$  : subtract 256

(And similar for 16 bit representation, 32 bit representation, etc.).

Two's complement addition:

(Some), only do not carry least bit.

Result can be wrong, but is right mod  $2^n$ .

(8 bit representation; mod  $2^8$ ).

E.g.

$$\begin{array}{r}
 01111111 = +127 \\
 00060001 = +1 \\
 \hline
 -128 = 10006000 \quad ? \quad 128
 \end{array}$$

? modulo 256 these are the same!

$$\begin{array}{r}
 10000000 \quad -128 \\
 10060000 \quad -128 \\
 \hline
 0 = 00000000 \quad \text{Should be} \\
 \quad \quad \quad -256.
 \end{array}$$

Mod 256 they are the same.



# The Internet Checksum.

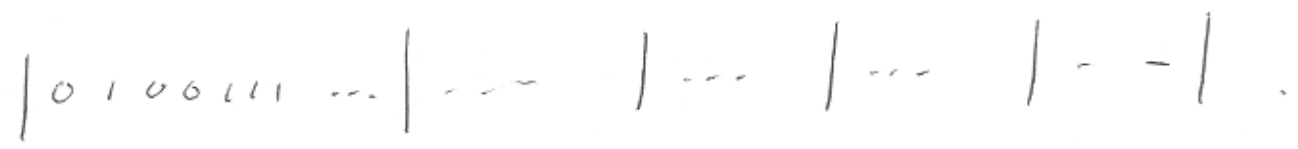
I'll do it for 16 bit representation.  
You can do it for general  $k$  bit representation.

16 bits is done on the Internet.

Arbitrary sequence of bits: (say a packet,  
or a header, or...)

0100111 ... 01010111

- (1) Append zeros at end to get integer number times 16 bits.
- (2) Divide up in  $k$  "16 bit words".



- (3) Add these 16 bit words using one's complement addition.
- (4) Take one's complement of result.
- (5) Append at end:  
Now we have  $(k+1)$  "16 bit words".
- (6) Send these  $(k+1)$  "16 bit words".  
(with or without the extra zeros: agree first).

How does the receiver check?

- (3) Check: (if necessary put zero back in).  
 Add all  $(k+1)$  16-bit words.  
 Result must be "0" =

1111 1111 1111 1111

(No need to repeat the procedure).

"Proof": Do it yourself.  
 (Maybe: end of semester).

This checksum detects all errors in  
 an odd number of bits,  
 and most errors of an even number  
 of bits. But not all. E.g.

x	y	z	u
a	!y	b	c

→

x	!y	z	u
a	y	b	c

is not detected.

There are better error detecting methods. 802.3 uses "CRC", 32 bits (Cyclic ~~Red~~ Redundancy Check).

This is better.  
Uses fancy math.  
End of semester.

There are several CRCs.

Typically: Detect all errors in odd number of bits.  
All errors localized to a stretch of 32 ~~bits~~ bits, ("error burst") (32? or 31?)  
Most other errors.

How are error detecting codes used?

At receiver:  
IF the test fails,  
throw packet on the floor.

possibly: send "NACK".  
(Usually not done).

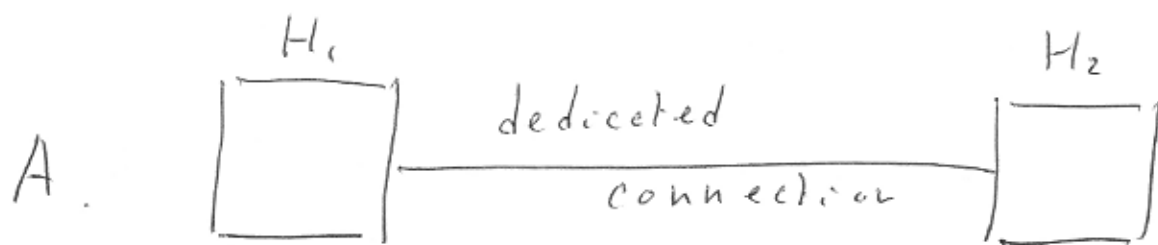
ACK: acknowledgement.

"I got it".

NACK: negative acknowledgement.

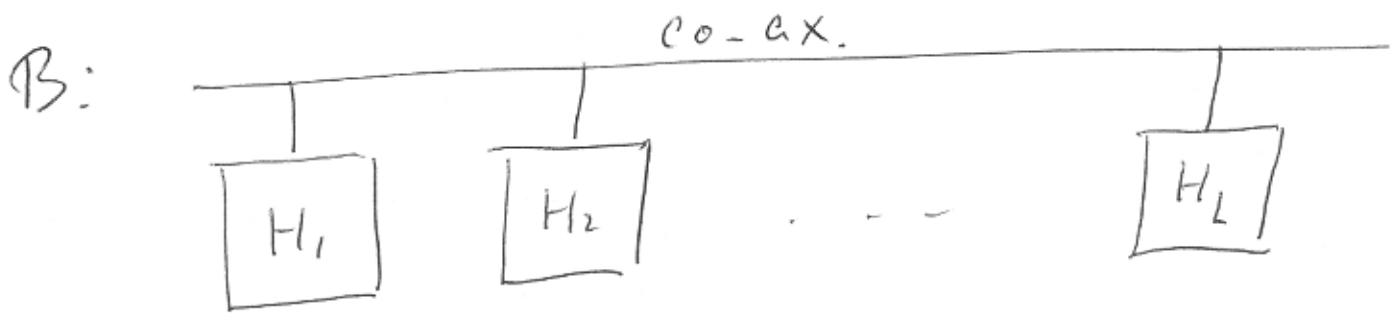
"I did not get it".

Why do most systems not use NACKs?



In case A, NACKs can be used -

"I got a packet, it Failed { CRC  
checksum "



Host  $i$  receives packet.

Checks CRC.

Fails.

"Maybe the error is in the ~~source~~ <sup>dest</sup> address. Is this packet really for me?"

"Maybe the error is in the ~~source~~ <sup>dest</sup> address. IF I send a NACK, maybe I will confuse somebody."

So: <sup>in case B,</sup> do drop packet,  
do not send NACK.

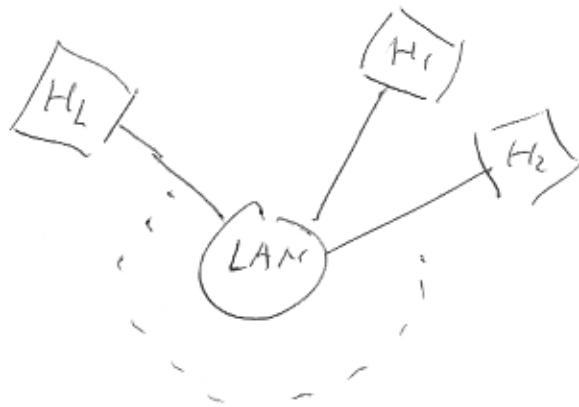
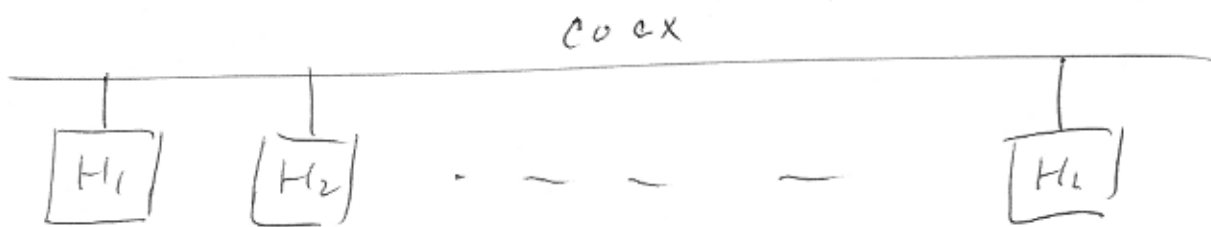
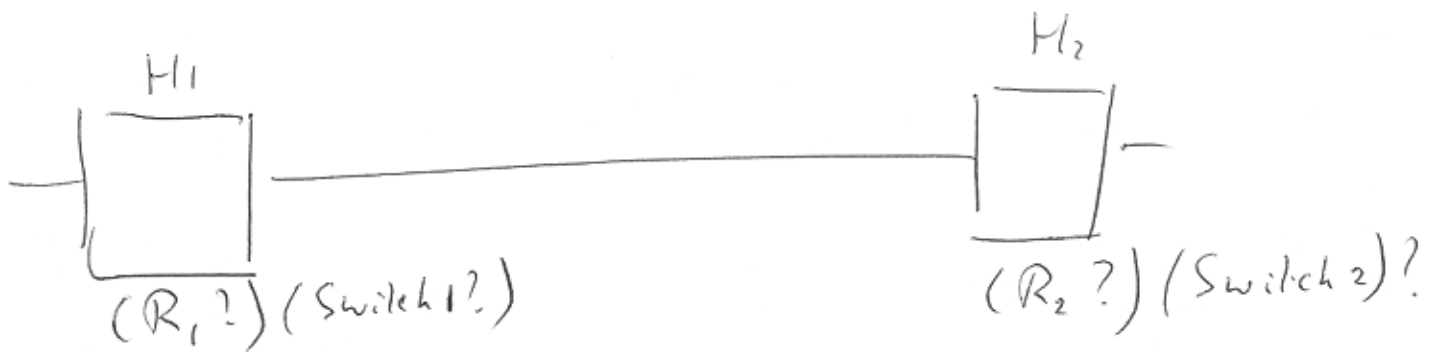
There are systems that use NACKs.

X.25 uses "NACK", there called "Reject".

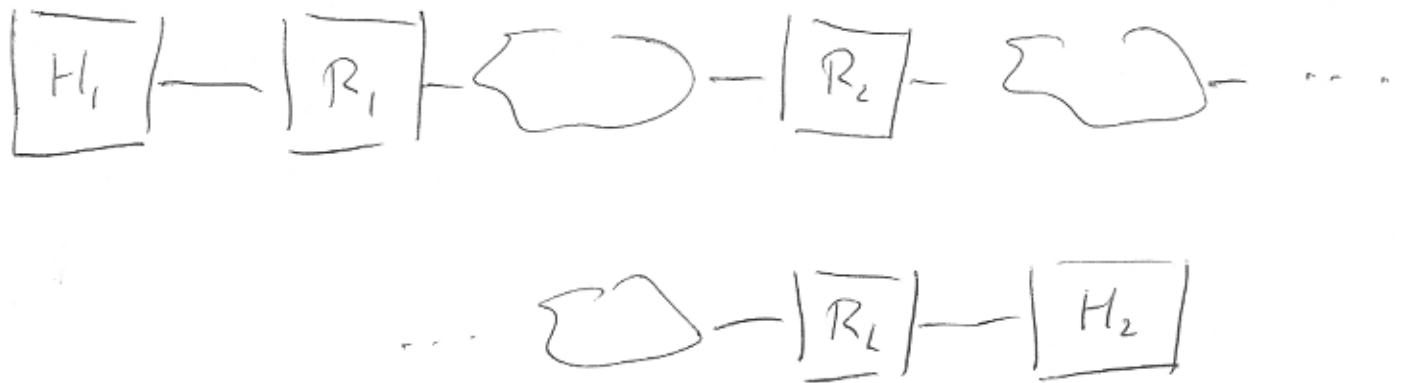
Elementary Data Link Protocols.

Tanenbaum p 200 etc.

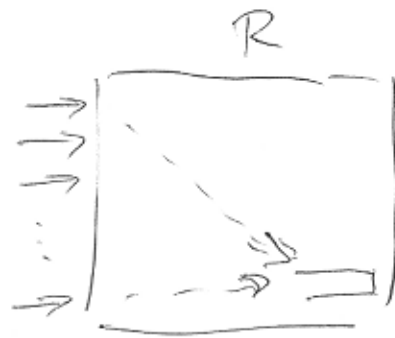
This story ~~is~~ applies to  
Data Link Protocols (Layer 2)



But it also applies to  
 "Transport Protocols" (Layer 4)



Routers may drop packets due to congestion.



("Focussed overload").

Issue :

Frames (packets) can get damaged.  
(CRC or Checksum Fails).

Frames (packets) can be dropped.  
(disappear into nowhere).  
e.g., congestion.

How do we build a  
Reliable system?

Acks, NACKs.



First: assume ~~to~~ ACKs as well as NACKs are used.

Simple system: "stop and wait".

Bad implementation:

At source:

1. Source sends Frame (or packet).

2. Waits for ACK or NACK.

3.   
 if ~~NACK~~ NACK: Retransmit, back to (2)   
 if ACK: back to (1)

At destination:

1. Wait for Frame.

2.   
 if good: send ACK

2.   
 if bad: send NACK.

Why is this implementation  
BAD ?

IF even a packet disappears  
without trace:  
both ~~the~~ sides wait Forever  
(dead-lock).

Solution: T.O.  
Time - Out

Simple "stop and wait",  
Improved implementation.  
(still not good!).

1. At time  $t$ , source sends Frame.  
Sets time-out for  $t + TO$ .  
( $TO$ : parameter to be chosen).
2. Source waits for ACK, NACK,  
or time-out, whichever happens  
first.
3. At time-out: (at time  $\tau$ )  
Re-transmit Packet (Frame)  
Set time-out for  $\tau + TO'$   
(Not necessarily  $TO' = TO$ ).
4. At NACK: (at time  $\tau$ ) Goto (2)  
Re-transmit packet (Frame)  
Set time-out for  $\tau + TO$  Goto (2)
5. IF ACK: (at time  $\tau$ )  
Transmit new packet.  
Set time-out for  $\tau + TO$  } "Goto 1".  
Goto 2.

At dest :

(1) Wait For Frame .

(2) if good : send ~~Act.~~ ACK

if bad : send NACK

Goto (1)

Is this system sound ?

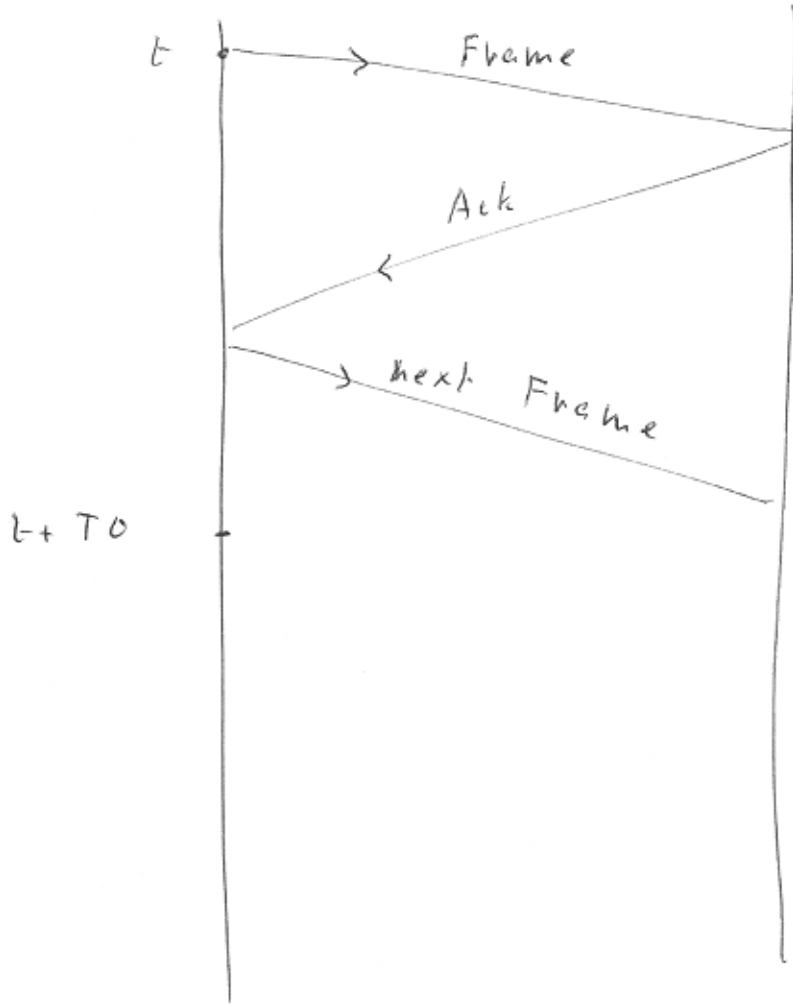
No !

At least : not if a "good" packet can get delayed .

Source

Dest.

94 ~~95~~  
95

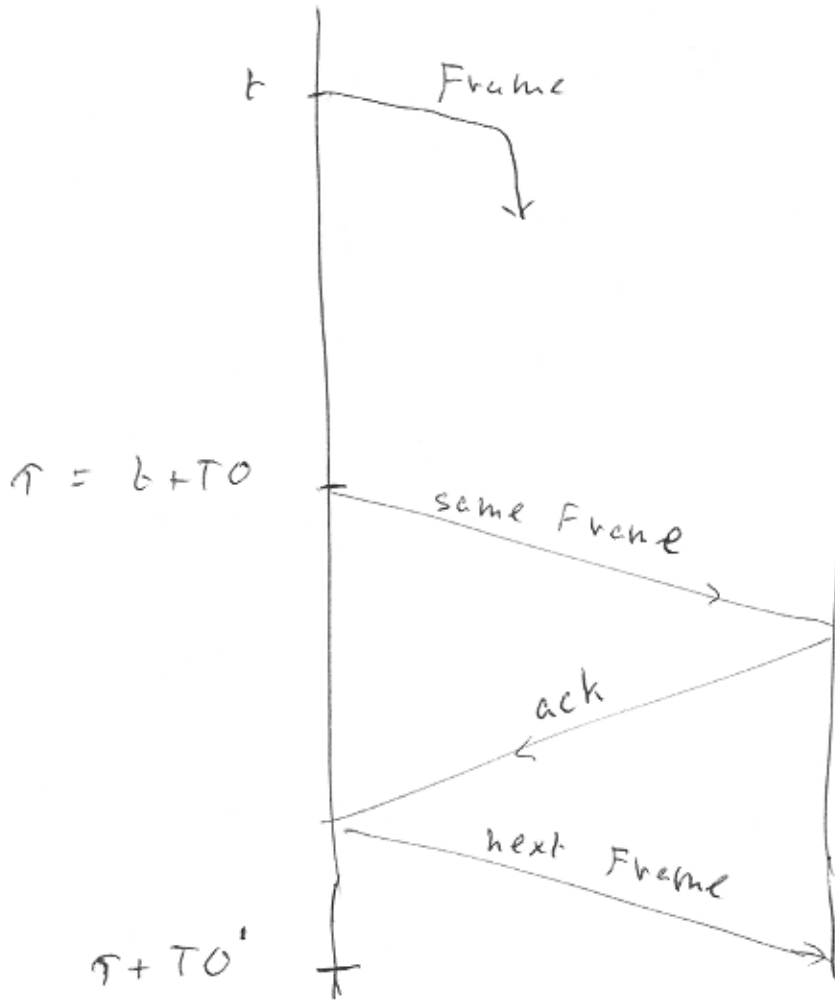


OK!

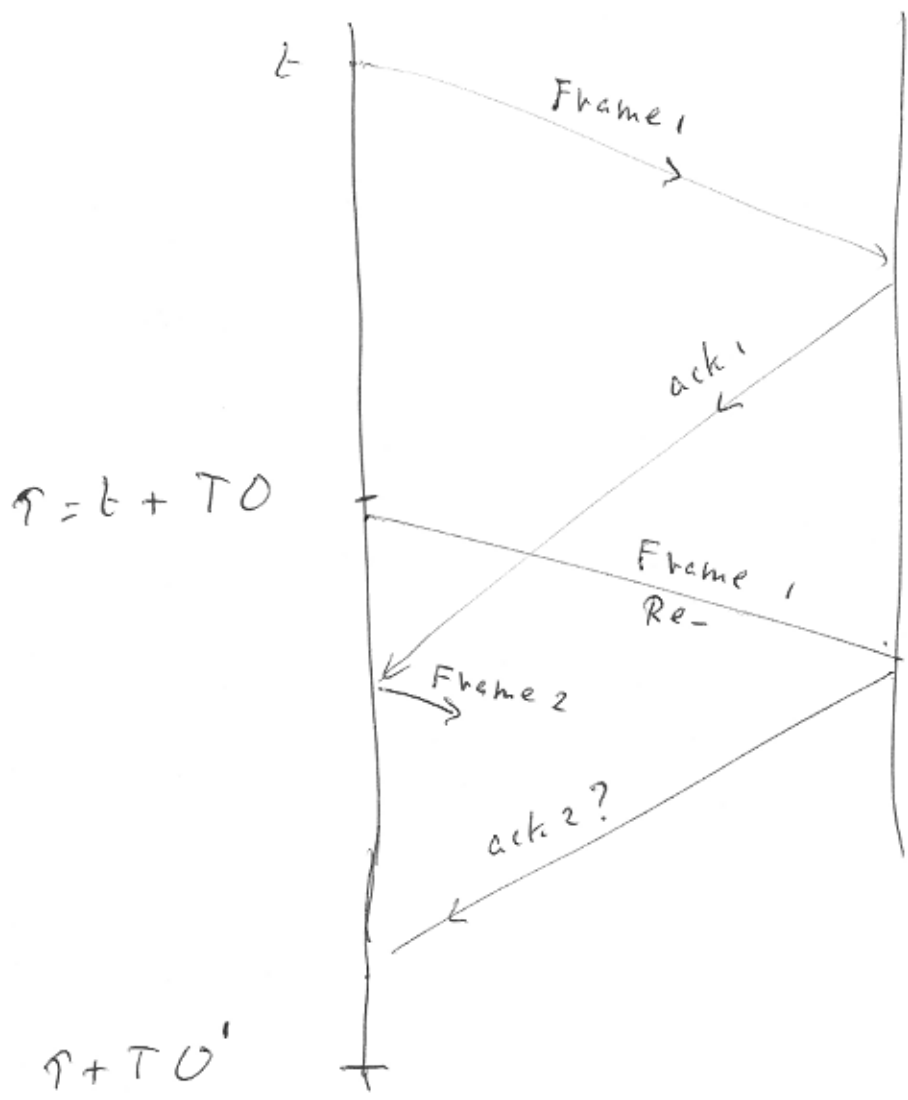
Source

Dest.

95 ~~96~~



Ok!



Delayed Data Frame (or Ack).

BAD

Not  
OK.

The destination gets Frame 1 twice but thinks it got Frames 1 and 2 : Error.

E.g. Email: a few tens or hundreds of characters will be repeated.

Data File: worse!

Solution :

Data Frames : number the Frames,  
(sequence number).

Include the sequence number in  
the Frame.

Acknowledgements :

Include sequence number of  
Frame being acknowledged.

NACK : better not include  
sequence number.  
could be wrong!